

Mark Scheme (Results)

January 2019

Pearson Edexcel International Advanced Level In Mechanics M3 (WME03/01)

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## **General Marking Guidance**

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively.
   Candidates must be rewarded for what they
  have shown they can do rather than
  penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

#### PEARSON EDEXCEL IAL MATHEMATICS

## **General Instructions for Marking**

- 1. The total number of marks for the paper is 75
- 2. The Edexcel Mathematics mark schemes use the following types of marks:
  - M marks: Method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
  - A marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
  - **B** marks are unconditional accuracy marks (independent of M marks)
  - Marks should not be subdivided.

#### 3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes.

- bod benefit of doubt
- ft follow through
- the symbol  $\sqrt{\phantom{a}}$  will be used for correct ft
- cao correct answer only
- cso correct solution only. There must be no errors in this part of the question to obtain this mark
- isw ignore subsequent working
- awrt answers which round to
- SC: special case
- oe or equivalent (and appropriate)
- d... or dep dependent
- indep independent
- dp decimal places
- sf significant figures
- \* The answer is printed on the paper or ag- answer given
- 4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.

- 5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.
- 6. If a candidate makes more than one attempt at any question:
  - If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
  - If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.
- 7. Ignore wrong working or incorrect statements following a correct answer.

# **General Principles for Mechanics Marking**

(But note that specific mark schemes may sometimes override these general principles)

- Rules for M marks: correct no. of terms; dimensionally correct; all terms that need resolving (i.e. multiplied by cos or sin) are resolved.
- Omission or extra g in a resolution is an accuracy error not method error.
- Omission of mass from a resolution is a method error.
- Omission of a length from a moments equation is a method error.
- Omission of units or incorrect units is not (usually) counted as an accuracy error.
- DM indicates a dependent method mark i.e. one that can only be awarded if a previous specified method mark has been awarded.
- Any numerical answer which comes from use of g = 9.8 should be given to 2 or 3 SF.
- Use of g = 9.81 should be penalised once per (complete) question.
  - N.B. Over-accuracy or under-accuracy of correct answers should only be penalised *once* per complete question. However, premature approximation should be penalised every time it occurs.
- Marks must be entered in the same order as they appear on the mark scheme.
- In all cases, if the candidate clearly labels their working under a particular part of a question i.e. (a) or (b) or (c),.....then that working can only score marks for that part of the question.
- Accept column vectors in all cases.
- Misreads if a misread does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, bearing in mind that after a misread, the subsequent A marks affected are treated as A ft
- Mechanics Abbreviations
  - M(A) Taking moments about A.
  - N2L Newton's Second Law (Equation of Motion)
  - NEL Newton's Experimental Law (Newton's Law of Impact)
  - HL Hooke's Law
  - SHM Simple harmonic motion
  - PCLM Principle of conservation of linear momentum
  - RHS, LHS Right hand side, left hand side.

# Jan 2019 IAL WME03 M3 Mark Scheme

Mark Scheme		
Question Number	Scheme	Marks
1.	$v\frac{\mathrm{d}v}{\mathrm{d}x} = \frac{7}{2} - 2x$	M1
	$\frac{1}{2}v^2 = \frac{7}{2}x - x^2 \ (+c)$	A1
	$x = 0  v = 3 \implies c = \frac{9}{2}$	A1
	$v = 0 \qquad 0 = \frac{7}{2}x - x^2 + \frac{9}{2}$	M1
	$2x^{2} - 7x - 9 = 0$ $(2x - 9)(x + 1) = 0$	M1
	x = 4.5 oe	Alcso
	By definite integration:	Aleso
	$v\frac{\mathrm{d}v}{\mathrm{d}x} = \frac{7}{2} - 2x$	M1
	$\int v  dv = \int \left(\frac{7}{2} - 2x\right) dx \Rightarrow \left[\frac{1}{2}v^2\right]_3^0 = \left[\frac{7}{2}x - x^2\right]_0^x$	A1A1
	$(0) - \frac{1}{2} \times 3^2 = \frac{7}{2} X - X^2  (-0)$	M1
	$2X^2 - 7X - 9 = 0 \implies X = 4.5$ oe	M1A1cso
		[6]
M1	For an equation of motion with the acceleration in the form $v \frac{dv}{dx}$ oe	
1411	dx	
	May be implied by sight of $(1/2)v^2$ after integration	
A1	Correct integration, constant not needed	
A1	Use $x = 0$ $v = 3$ to obtain $c = 9/2$	
M1	Substitute $v = 0$ in their expression for $v^2$ or $v$ . Award M0 if this expression	
M1	Solve the resulting <b>3TQ</b> in $x$ only, by any valid means. Must reach $x =$ (les scores M0)	s than 3 terms
A1cso	Correct value for x obtained from correct working. If $x = -1$ is seen it must be <b>By definite integration:</b>	e eliminated.
M1	For an equation of motion as above	
<b>A1</b>	Correct integration, ignore limits	
A1	Correct limits, as shown or both sets reversed	
M1	Substitute their limits, zeros need not be shown	3.60\
M1	Solve the resulting <b>3TQ</b> by any valid means. Must reach $X =$ (less than 3 to	erms scores M0)
A1cso NB	Correct value for x obtained from correct working.	
IND	Solving a 3TQ, Calculator solutions: Correct equation: correct answer implies correct meth	and (Incorrect
	answer M0) -1 need not be seen. Incorrect equation: No working, award M0	*
	By formula: Correct general formula seen and used (even with incorrect sub) scores M1.	
	With no general formula, award M1 if the sub in the formula is correct for the	

Question Number	Scheme	Marks
2	$R(\uparrow) T_A \cos 60^\circ = T_B \cos 60^\circ + mg$	M1A1
	$T_A = T_B + 2mg$	
	NL2 along radius: $T_A \cos 30^\circ + T_B \cos 30^\circ = ma \cos 30^\circ \omega^2$	M1A1A1
	$T_A + T_B = ma\omega^2$	
	$T_A = \frac{1}{2} \left( ma\omega^2 + 2mg \right)$	dM1A1
	$T_B = \frac{1}{2} \left( ma\omega^2 - 2mg \right)$	A1
	$T_A = \frac{1}{2} \left( ma\omega^2 + 2mg \right) < 3mg$	
	$\omega^2 < \frac{4g}{a}$	M1
	$T_B = \frac{1}{2} \left( ma\omega^2 - 2mg \right) > 0$	
	$\omega^2 > \frac{2g}{a}$	M1
	$S = \frac{2\pi}{\omega} \Rightarrow \pi \sqrt{\frac{a}{g}} < S < \pi \sqrt{\frac{2a}{g}} \qquad k = 2$	dM1A1cso (12)
		[12]
M1	Resolving vertically. Both tensions resolved but can be sin or cos of 30 or 60 is an accuracy organ.	Omission of $g$
<b>A1</b>	is an accuracy error. Fully correct equation	
M1	Attempt NL2 along the radius. Both tensions resolved but can be sin or cos of 30° or 60°.	
A1	Acceleration in either form. Allow with $r$ instead of $a \cos 30^{\circ}$ Both forces correct. ( $r$ or $a \cos 30^{\circ}$ )	
A1	Fully correct equation with acceleration in $a \cos 30^{\circ} \times \omega^{2}$ form	
dM1	Solve the equations for either tension in terms of $m, a, \omega$ (g may be missing)	. Depends on
A 4	both M marks above.	
A1 A1	Either tension correct Second tension correct	
	Use their $T_A < 3mg$ to obtain an inequality for $\omega^2$ (or $\omega$ ) in terms of $g$ and $g$	a
M1	Use of $\leq$ scores M0	
M1	Use their $T_B > 0$ to obtain an inequality for $\omega^2$ (or $\omega$ ) in terms of $g$ and $a$	
1411	Use of $\geqslant$ scores M0	
dM1	Use $S = \frac{2\pi}{\omega}$ with <b>both</b> inequalities to obtain a final result. Depends on the two	wo M marks for
Alcso	the inequalities.  Correct final result as shown in the question from fully correct working. Value shown explicitly.	tue of $k$ need not

Question Number	Scheme	Marks
	Solutions using $\omega = \frac{2\pi}{S}$ (or $\frac{2\pi}{T}$ )	
	$R(\uparrow) T_A \cos 60^\circ = T_B \cos 60^\circ + mg$	M1A1
	$T_A = T_B + 2mg$	
	$T_A + T_B = ma \left(\frac{2\pi}{S}\right)^2$	M1A1A1
	$T_A = \frac{1}{2} \left( ma \left( \frac{2\pi}{S} \right)^2 + 2mg \right)$	dM1A1
	$T_B = \frac{1}{2} \left( ma \left( \frac{2\pi}{S} \right)^2 - 2mg \right)$	A1
	$T_A = \frac{1}{2} \left( ma \left( \frac{2\pi}{S} \right)^2 + 2mg \right) < 3mg$	
	$S^2 > \frac{\pi^2 a}{g}$	M1
	$T_B = \frac{1}{2} \left( ma \left( \frac{2\pi}{S} \right)^2 - 2mg \right) > 0$	
	$S^2 < rac{\pi^2 a}{2g}$	M1
	$S^{2} < \frac{\pi^{2} a}{2g}$ $\Rightarrow \pi \sqrt{\frac{a}{g}} < S < \pi \sqrt{\frac{2a}{g}} \qquad k = 2$	dM1A1cso (12)
NB	The final M mark is for using $S = \frac{2\pi}{\omega}$ and must only be awarded when both have been used to obtain the final result.	inequalities
	<b>Solutions using</b> $T_A=3mg$ and $T_B=0$ :	
	If <b>2 cases</b> are considered, (i) with $T_A = 3mg$ and (ii) with $T_B = 0$ , first 8 marks are available	
	but no more. If equations are formed including $T_A$ =3 $mg$ and $T_B$ = 0 in the same equation marks gained before the sub is made but once the sub is made there are no furnitarial available.	

Question Number	Scheme	Marks
3(a)	$v^{2} = \omega^{2} \left( a^{2} - \frac{a^{2}}{4} \right) = \frac{3a^{2}\omega^{2}}{4}$ $\frac{27a^{2}}{4} = \frac{3a^{2}\omega^{2}}{4}$	
		M1
	$\omega = 3$	A1
	$Period = \frac{2\pi}{3}$	A1ft (3)
(b)	Max mag of accel = $a\omega^2$	
	45 = 9a, $a = 5$	M1,A1ft (2)
(c)	$x = a \sin \omega t$ $\dot{x} = a\omega \cos \omega t$ (or $x = a \cos \omega t$ $\dot{x} = -a\omega \sin \omega t$ )	
	$\dot{x}_{\text{max}} = 5 \times 3 = 15 \text{ (m s}^{-1})$	M1A1ft (2)
	<b>OR</b> $v_{\text{max}} = a\omega = 5 \times 3 = 15 \text{ (m s}^{-1})$ M1A1ft (2)	
(d)	Time A to C $\frac{1}{2}a = a\cos\omega t \Rightarrow \frac{1}{2} = \cos 3t$	
	$t_{AC} = \frac{1}{3}\cos^{-1}\left(\frac{1}{2}\right) = \frac{\pi}{9}  (0.3490)$	M1A1
	Time A to D $\frac{\pi}{9} + \frac{2\pi}{12} = \frac{5\pi}{18}$	
	$x_D = 5\cos\left(3 \times \frac{5\pi}{18}\right) = -\frac{5\sqrt{3}}{2} \left(=-4.330\right)$	M1A1
	Distance $CD \frac{5}{2} + \frac{5\sqrt{3}}{2} = \frac{5}{2} (1 + \sqrt{3})$ or 6.8 (m) (or better)	A1ft (5) [12]

Question Number	Scheme	Marks
(a)		
M1	Use of $v^2 = \omega^2 (a^2 - x^2)$ with $v = \frac{3a\sqrt{3}}{2}$ , $x = \frac{1}{2}a$ , amp = a (or any other com	plete method)
<b>A1</b>	Correct value for $\omega$	
A1ft	Correct period, follow through their $\omega$	
(b)		
M1 A1ft	Use max mag of accel = $a\omega^2$ with their $\omega$	
(c)	a = 5	
M1	Use either method shown with their values of a and $\omega$ to obtain a value for the	ne max speed
A1ft	$v_{\text{max}} = 15 \text{ (m s}^{-1})$	
(d)	,	
M1	Attempt time A to C with their value of $\omega$ and $x = \frac{1}{2}a$ or half their amp. Must reach a value	
A1	for t using radians Correct time, exact or min 3 sf (no penalty for using an incorrect amp) The above 2 marks can be awarded for a time even if no indication of which time the are finding (ie not stated to be time from end to C or centre to C. Following marks can only be	
M1	awarded if work is consistent with their work for these 2 marks. Add $\frac{1}{4}$ period and use this time to obtain a value for $x$ at $D$ using their value for $a$ or just $a$	
A1	Correct value of $x$ exact or min 3 sf or a multiple of $a$	ioi a oi just a
A1ft	Correct distance $CD$ , follow through their $x_D$ Must be positive Min 2 sf for	decimal
ALT (d)	Time C to centre $O$ $\frac{1}{2}a = a \sin \omega t \Rightarrow \frac{1}{2} = \sin 3t$	
	$t_{CO} = \frac{1}{3} \sin^{-1} \left( \frac{1}{2} \right) = \frac{\pi}{18}  (0.1745)$	M1A1
	Time $O$ to $D$ $\frac{\pi}{6} - \frac{\pi}{18} = \frac{\pi}{9}$	
	$OD = a\sin\frac{\pi}{3} = \frac{\sqrt{3}}{2}a$	M1A1
	Distance $CD \frac{5}{2} + \frac{5\sqrt{3}}{2} = \frac{5}{2} (1 + \sqrt{3})$ or 6.83 (m)	A1ft

Question Number	Scheme	Marks
4(a)	$A \longrightarrow B$	
	$R(\uparrow): 2T\cos\theta = 2mg$	M1A1
	$\cos \theta = \frac{3}{5}$ (or other correct trig function)	B1
	$T = \frac{\lambda \times l}{4l} \text{ or } \frac{\lambda \times 0.5l}{2l}$ $T = \frac{5mg}{3} = \frac{\lambda}{4}$ $\lambda = \frac{20}{3}mg  *$	M1A1
	$T = \frac{5mg}{3} = \frac{\lambda}{4}$	
	$\lambda = \frac{20}{3} mg  *$	M1A1cso (7)
(b)	Dist below $AB = l\sqrt{3^2 - 2^2} = l\sqrt{5}$ (or 2.23 <i>l</i> )	B1
	EPE at start: $=\frac{\lambda \times (2l)^2}{2 \times 4l} = \frac{20mg}{3} \times \frac{(2l)^2}{8l}  \left(=\frac{10mgl}{3}\right)$	M1A1
	GPE gained if P reaches $AB = 2mgl\sqrt{5} = 4.47mgl$	B1
	$\frac{10}{3}$ < 4.47	M1
	P cannot reach the line $AB$	Alcso (6)
		[13]

Question Number	Scheme	Marks
(a)M1	Resolve vertically. Must have 2 tensions, both resolved and (2)m or (2)mg no	ot resolved
<b>A1</b>	Fully correct equation	
<b>B</b> 1	Correct sine, cosine or tangent, seen explicitly or used in an equation	
M1	Use Hooke's law for the full string or half string with their attempt at the extension	ension
A1	Fully correct equation	
M1	Eliminate T between their 2 equations to obtain an expression for $\lambda$	
A1cso	Correct given result obtained from correct working	
(b) B1	Correct initial distance below the level of AB	
M1	Calculate the initial EPE, formula to be of the form $\frac{\lambda x^2}{k \times \text{natural length}}$ , $k = 2$	or 1.
	Must use the full string or 2 x half strings	
A1	Correct initial EPE Need not be simplified	
B1	GPE gained if P reaches AB	
M1 A1cso	Compare the initial EPE with the GPE – using exact or decimal results Correct work and a conclusion (exact or decimals results used)	
AICSU	Correct work and a concrusion (exact of decimals results used)	
	Alternatives for last 3 marks:	
ALT1	Assume $P$ stops at distance $x$ below $AB$	
B1	GPE gained $2mg(l\sqrt{5}-x)$	
M1	Attempt an energy equation with initial and final KE zero and show it has a proot	positive, real
A1cso	$\frac{10mgl}{3} - 2 \times \frac{20mg}{3} \times \frac{\left(\sqrt{4l^2 + x^2} - 2l\right)^2}{4l} = 2mg\left(l\sqrt{5} - x\right)$ Final KE must be 0, 2 EPE terms needed Correct work and a conclusion	
ALT 2	Assume final extension is $x$ Similar work may be seen with final extension $x$	2x
B1	GPE gained $2mg\left(l\sqrt{5}-\sqrt{\left(2l+\frac{x}{2}\right)^2-4l^2}\right)$	
M1	Attempt an energy equation with initial KE zero and show it has a positive, r	eal root
	$\frac{10mgl}{3} - \frac{20mg}{3} \times \frac{x^2}{4l} = 2mg\left(l\sqrt{5} - \sqrt{\left(2l + \frac{x}{2}\right)^2 - 4l^2}\right)$	
A1cso	Final KE must be 0, 2 EPE terms needed Correct work and a conclusion	

Question Number	Scheme	Marks
ALT3 B1 M1	Assume P stops after rising a distance x  GPE gained 2mgx  Attempt on energy equation with initial and final VE zero and show it has a	mocitivo mod
MII	Attempt an energy equation with initial and final KE zero <b>and</b> show it has a root $\frac{10mgl}{3} - 2 \times \frac{20mg}{3} \times \frac{\left(\sqrt{4l^2 + \left(l\sqrt{5} - x\right)^2} - 2l\right)^2}{4l} = 2mgx$	positive, real
A1cso	Final KE must be 0, 2 EPE terms needed Correct work and a conclusion	
M1 A1cso	Alternative for last 2 marks: Attempt an energy equation including the KE at level of $AB$ and solve for $v^2 < 0$ so $P$ cannot reach the level of $AB$ (Equation must be correct)	
	<b>Warning:</b> in (b), use of HL with extension 2 <i>l</i> can also lead to the "correct" re M0 as it is not an energy solution. (May possibly gain the B marks but this is	-

Question Number	Scheme	Marks
5(a)	$Vol = (\pi) \int_{\frac{3}{5}r}^{r} (r^2 - x^2) dx = (\pi) \left[ r^2 x - \frac{1}{3} x^3 \right]_{\frac{3}{5}r}^{r}$	M1A1
	$= (\pi) \left( r^3 - \frac{1}{3} r^3 - \left( \frac{3}{5} r^3 - \frac{9}{125} r^3 \right) \right) \left( = \frac{52}{375} (\pi) r^3 \right)$	M1
	$(\pi) \int_{\frac{3}{5}r}^{r} x (r^2 - x^2) dx = (\pi) \left[ \frac{1}{2} r^2 x^2 - \frac{1}{4} x^4 \right]_{\frac{3}{5}r}^{r}$	M1A1
	$= (\pi) \left( \frac{1}{2} r^4 - \frac{1}{4} r^4 - \left( \frac{9}{50} r^4 - \frac{81}{2500} r^4 \right) \right) \left( = \frac{64}{625} (\pi) r^4 \right)$ $\overline{x} = \frac{\int xy^2 dx}{\int y^2 dx} = \frac{\frac{64}{625}}{\frac{52}{375}} r$ $= \frac{48}{65} r  *$	M1
	$\overline{x} = \frac{\int xy^2 dx}{\int y^2 dx} = \frac{\frac{64}{625}}{\frac{52}{375}}r$	M1
	$=\frac{48}{65}r$	Alcso (8)
(b)	Bowl alone: Mass ratio $6^3$ $5^3$ 91	
	Dist from $A: \frac{3}{8} \times 6 = \frac{3}{8} \times 5 = \overline{y}$	
	$216 \times \frac{3}{8} \times 6 - 125 \times \frac{3}{8} \times 5 = 91\overline{y}$	M1A1A1
	$\overline{y} = 2.7651$ $\left(\frac{2013}{728}, 2\frac{557}{728}\right)$	A1
	Bowl and liquid: Mass ratio 5 2 7	
	Dist from $A$ : $2.7651$ $\frac{48}{13}$ $\overline{z}$	B1 (48/13)
	$7\overline{z} = 5 \times 2.7651 + \frac{48}{13} \times 2$	M1A1ft
	$\overline{z} = 3.030 = 3.03$ cm	A1 (8) [16]
ALT	Find mass of whole hemisphere and part cut away in terms of $M$ and use a single moments equation (see end)	[10]

Question Number	Scheme	Marks
(a)	Lamina scores 0/8. If no evidence of algebraic integration seen, only the last M mark is available.	
M1 A1 dM1	Attempt the volume integral, $\pi$ and limits not needed (ignore any shown) Correct integration, $\pi$ and limits not needed (ignore any shown) Substitute the correct limits in their result. Evidence of substitution must be son previous M mark	seen. Depends
M1	Attempt $\int xy^2 dx$ , $\pi$ and limits not needed (ignore any shown)	
A1 dM1	Correct integration, $\pi$ and limits not needed (ignore any shown) Substitute the correct limits in their result. Evidence of substitution must be son previous M mark	een. Depends
M1	Use $\overline{x} = \frac{\int xy^2 dx}{\int y^2 dx}$ with their previous results (need not be simplified results). $\pi$ in both or	
A1cso (b) M1  A1 A1 A1 B1 M1  A1ft A1	neither integral Correct final ( <b>given</b> ) result obtained from fully correct working.  Attempt a moments equation with the <i>difference</i> of two hemispheres. Dimens hemispheres must be correct.  Correct masses or ratio of masses Correct distances Correct distances Correct distance for the bowl – exact or decimal For the correct distance of the c of m of the liquid from A Attempt a moments equation – bowl and liquid added. Must attempt the distalliquid ie we are looking for a numerical distance, not just a letter and must be evidence of calculating the c of m of the bowl (M mark for this may have been correct equation, follow through their distances (ie 48/13 and c of m of bowl Correct answer from correct working. Must be 3 sf	ance for the nave shown en lost)

Question Number	Scheme	Marks
ALT (b)	Vol of bowl = $\frac{2}{3}\pi (6^3 - 5^3) = \frac{2}{3}\pi \times 91$	
	$\frac{2}{3}\pi\rho\times91=5M$	B1
	Mass ratio $6^3$ $5^3$	
	Mass ratio $6^{3}$ $5^{3}$ $6^{3} \times \frac{5}{91}M$ $5^{3} \times \frac{5}{91}M$ $2M$ $7M$	M1A1A1
	Dist from $A: \frac{3}{8} \times 6$ $\frac{3}{8} \times 5$ $\frac{48}{13}$ $\overline{y}$	B1(48/13)
	$6^{3} \times \frac{5}{91} M \times \frac{3}{8} \times 6 - 5^{3} \times \frac{5}{91} M \times \frac{3}{8} \times 5 + 2M \times \frac{48}{13} = 7M \overline{y}$	M1A1ft
	$\overline{y} = 3.030 = 3.03$	A1 (8)
B1	For a correct equation connecting the mass of the bowl and 5 <i>M</i> . Award if 5 <i>M</i> seen used correctly in at least one term in their equation.	$_{01}^{\prime}M$ or $\frac{5}{91}$ is
	Enter as the first A mark on e-PEN	
<b>M</b> 1	For attempting the mass ratio for the 4 parts needed including their "5/91"	
A1A1	Deduct one per error	
B1	For 48/13	
M1	Attempt a moments equation with 4 terms and correct signs. An attempt at t	
	the parts based on the mass of the bowl being 5M must have been seen even	if this attempt
A1ft	failed to qualify for the first M mark.  Correct equation, follow through their masses and distances (ie 48/13 and co	of m of hovel)
AIII A1	Correct answer from correct working. Must be 3 sf	11 11 01 00W1)
111	Correct answer from correct working, widst oc 3 si	

Question Number	Scheme	Marks
6(a)	Energy to $B: \frac{1}{2}m \times \frac{7ag}{2} - \frac{1}{2}mv^2 = mga$	M1A1
	NL2 along rad at $B: R = m \frac{v^2}{a}$	M1A1
	$R = \frac{3mg}{2}$	A1cao (5)
(b)	Energy A to $C: \frac{1}{2}m \times \frac{7ag}{2} - \frac{1}{2}mV^2 = mga(1 + \cos\theta)$	M1A1
	OR energy B to $C: \frac{1}{2}m \times \frac{3ag}{2} - \frac{1}{2}mV^2 = mga\cos\theta$	
	NL2 along rad at $C$ : $mg \cos \theta = m \frac{V^2}{a}$	M1A1
	Solve for $\theta$ : $\frac{1}{2}m \times \frac{7ag}{2} - \frac{1}{2}mga\cos\theta = mga(1+\cos\theta)$	dM1
	$\cos\theta = \frac{1}{2} \qquad \left(\theta = 60^{\circ}\right)$	A1
	Horiz motion: $s = a \sin \theta$ , speed = $V \cos \theta$	
	$t = \frac{a\sin\theta}{V\cos\theta} = \sqrt{\frac{2}{ag}} \times a\sqrt{3} = \sqrt{\frac{6a}{g}}$	M1
	Vert motion: $s = -V \sin \theta \times t + \frac{1}{2}gt^2$	M1
	$s = -\sqrt{\frac{ag}{2}} \times \frac{\sqrt{3}}{2} \times \sqrt{\frac{6a}{g}} + \frac{1}{2}g \times \frac{6a}{g}, = -\frac{3a}{2} + 3a = \frac{3a}{2}$	A1,A1
	Horiz dist A to C: $s = a \sin 60^\circ = \frac{a\sqrt{3}}{2}$	
	sufficient that this was used to find the time	
	Vert dist A to C: $s = \frac{3a}{2}$	
	$\therefore$ Strikes surface at $A$	A1cso (11) [16]

Question Number	Scheme	Marks
(a)M1	Attempt an energy equation from start to B. Must have 2 KE terms and one PE term	
A1	Fully correct equation	
M1	Attempt an equation of motion along the radius at <i>B</i> . Acceleration can be in either form.	
A 1	Only force to be the reaction.	
A1 A1cao	Fully correct equation, acceleration as shown. Eliminate $v^2$ to obtain the expression for the reaction at B.	
(b)	Eliminate V to obtain the expression for the reaction at B.	
M1	Attempt an energy equation from start to C. Must have 2 KE terms and a PE term which includes a trig function. PE may be expressed as 2 separate terms	
A1	Fully correct equation	
M1	Attempt an equation of motion along the radius at <i>C</i> . The reaction may be included initially but must become 0 before this mark can be awarded. Weight must be resolved; acceleration can be in either form.	
<b>A1</b>	Fully correct equation, acceleration as shown.	
dM1	Eliminate $V$ and obtain a value for $\cos \theta$ . Depends on the 2 previous M marks of (b)	
A1	Correct value for $\cos \theta$ . Award if seen explicitly or implied by subsequent working.	
M1	Use the horizontal motion to obtain the time to travel a horizontal distance $= a \sin \theta$ , with their $\theta$ . Speed must be resolved. Time obtained must be a function of $a$ and $g$ only.	
M1	Use $s = ut + \frac{1}{2}at^2$ to obtain an expression for the vertical distance at time t. Acceleration to	
A1 A1	be $g$ and initial speed to be a component of their $V$ . (trig function or its value allowed here) Correct equation in $a$ , $g$ and $s$ Correct vertical distance	
A1cso	State that or use the horizontal distance A to C is $a \sin 60^\circ = \frac{a\sqrt{3}}{2}$ and the vertical distance A	
	to C is $(3a)/2$ so the particle strikes the surface at A. All work must be correct.	
ALT	For the last 4 marks: Find time to travel $3a/2$ vertically down from $C$ :	
	Vert motion: $s = -V \sin \theta \times t + \frac{1}{2}gt^2$	M1
	$\frac{3a}{2} = -\sqrt{\frac{ag}{2}} \times \frac{\sqrt{3}}{2}t + \frac{1}{2}gt^2, \implies t = \sqrt{\frac{6a}{g}}$	A1,A1
	Same time horiz and vertically so strikes surface at A	Alcso
M1	Use $s = ut + \frac{1}{2}at^2$ to obtain an expression for the time to travel $\frac{3a}{2}$ vertically. Acceleration	
A 1	to be $g$ and initial speed to be a component of their $V$ . (trig function or its value allowed here)	
A1	Correct equation in $a$ , $g$ and $t$	
<b>A1</b>	$t = \sqrt{\frac{6a}{g}}$	
A1cso	State that the horizontal and vertical times are the same, so the particle strikes the surface at	
***	A. All work must be correct.	
NB	$\theta$ is defined in the question as the angle with the vertical. If the angle with the horiz is	
	called $\theta$ but otherwise <i>totally</i> correct, deduct A mark for $\cos \theta$ and the final a mark.	
	If there are errors in the working, mark as scheme.	

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